# 1,3-Dipolar Character of Six-membered Aromatic Rings. Part 38. ${ }^{1}$ FMO Treatment of Peri-, Site, Regio, and Stereo-selectivity, and Relative Reaction Rates of Cycloaddition Reactions 

By Alan R. Katritzky * and Nicholas Dennis, School of Chemical Sciences, University of East Anglia, Norwich NR4 7TJ<br>Max Chaillet,* Christiane Larrieu, and Mohamed El Mouhtadi, Laboratoire de Chimie Structurale, Université de Pau et des Pays de l'Adour, B.P. 523, Pau, France


#### Abstract

The kinetic rates and peri-. site, regio-, and stereo-selectivity of the reactions of variously 1 -substituted 3 -oxidopyridiniums have been correlated by FMO theory. Regioselectivity is well explained by the standard perturbation treatment, but for correlation of the relative rates it is necessary to use the simpler equation of Sustmann. For the most part, stereoselectivity is well explained by a simple monopole repulsion treatment. Peri- and site selectivity are also discussed and are well correlated for reactions of dienes but not for fulvenes.


Previous papers of this series demonstrated that approximate CNDO/2 calculations on 1-methyl-3-oxidopyridinium ( 1$)^{2}$ rationalised the site, peri-, regio-, and stereo-selectivity of olefinic dipolarophile cycloadditions of type $(1,2,3,5,6,7) \longrightarrow(9)(c f$. ref. 3$)$. We now report more precise calculations and compare them with these selectivities and with kinetic rates (already reported in ref. 4).
Molecular Geometries.-We have used the same bond lengths and angles for the pyridinium ring of the betaines as previously justified. ${ }^{2}$ The bond lengths and angles for the betaine $N$-substituents and dipolarophiles utilised are given in formulae (10)-(13) [geometry (11) was also used for 4 -pyridyl]. For the 5 -nitro-2-pyridyl, 4,6-dimethylpyrimidin-2-yl, and for the 4,6 -dimethoxy(and 4,6-diphenyl-)triazin-2-yl substituents, we have used in the calculations the corresponding unsubstituted heteroaryl substituents (11)-(13) respectively.

(1) $R=M e$
(2) $R=H$
(3) $\mathrm{R}=\mathrm{Ph}$
(4) $R=4$ - Pyridyl
(5) $R=2$ - Pyridyl
(6) $R=$ Pyrimidin $-2-y l$
(7) $R=$ Triazin-2-yl
(8) $R=\beta$-Formylvinyl

This approximation is needed because of considerations of calculation time: the neglect of methyl substituents should have little effect; neglecting the 5 -nitro-group is expected to give a less reactive molecule whereas neglecting two methoxy-groups should give a more reactive molecule (the effects of phenyl substitution are less easily predicted). $\dagger$

[^0]As will become clear, the orbital energies in the 1 -aryl3 -oxidopyridiniums are considerably affected by the dihedral angle between the pyridine ring and the $N$-aryl


(10)

(11)

(12)

(13)

For (10), cf. I. L. Karle, J. Chem. Phys., 1952, 20, 65; J. N. Murrell, V. M. S. Gil, and F. B. Van Duijneveldt, Rec. Trav. chim. 1965, 84, 1399; for (11), B. Bak, L. Hansen-Nygaard, and J. Rastrup-Andersen, J. Mol. Spectroscopy, 1958, 2, 361; for (12), P. J. Wheatley, Acta Cryst., 1960, 13, 80; for (13), ref. 7, and P. J. Wheatley, Acta Cryst., 1955, 8, 224.
ring. For the $N$-phenyl and 4-pyridyl substituents we have taken $30^{\circ}$ for this angle: i.e. near the values for biphenyls. ${ }^{5}$ For the $N$-(pyrimidin-2-yl) and $N$-(triazin2 -yl) substituents, we have taken $0^{\circ}: X$-ray studies of 3,6-diphenyl-s-tetrazine, ${ }^{6}$ and 2,4,6-tris-( $p$-chlorophenyl)-

Table 1
Sources of geometry for dipolarophiles

| Dipolarophile | Ref. | Dipolarophile | Ref. |
| :--- | :---: | :--- | :---: |
| Acrylonitrile | $a$ | Cyclohexene | $h$ |
| n-Butyl vinyl ether | $b$ | Indene | $i$ |
| Methyl acrylate | $c$ | Cyclopentadiene | $j$ |
| Propene | $d$ | 1,1-Dimethylfulvene | $k$ |
| $s$-trans-Butadiene | $e$ | Allyl alcohol | $l$ |
| $s$-cis-Butadiene | $f$ | Vinyl acetate | $b, c$ |
| Difluoroketen | $g$ |  |  |

${ }^{a}$ M. Rouault and C. St.-Arnaud, Canad. J. Phys., 1957, 35, 504. ${ }^{b}$ S. Samdal and H. M. Seip, J. Mol. Structure, 1975, 28 , 193 (data obtained for methyl vinyl ether). 'G.' Williams, N. L. Owen, and J. Sheridan, Trans. Faraday Soc., 1971, 67, 922. ${ }^{d}$ D. R. Lide, jun., and D. E. Mann, J. Chem. Phys., 1957, 27,868 . ${ }^{e}$ A. Almenningen, O. Bastiansen, and M. Traetteberg, Acta Chem. Scand., 1958, 12, 1221. ${ }^{f}$ L. A. Burke, G. Leroy, and M. Sana, Theor. Chim. Acta, 1975, 40, 313. O J. Sheridan in 'Advances in Molecular Spectroscopy,' ed. A. Mangini, Pergamon, London, 1962, Vol. 1, p. 139; V. W. Laurie and D. T. Pence, J. Chem. Phys., 1963, 38, 2693 (data obtained by combining $\mathrm{CH}_{2}: \mathrm{C}: \mathrm{O}$ and $\mathrm{CH}_{2}: \mathrm{CF}_{2}$ ). ${ }^{n} \mathrm{~T}$. Ogata and K . Kozima, Bull. Chem. Soc. Japan, 1969, 42, 1263. 'J. F. Southern, Diss. Abstr. Int. B, 1973, 33, 3586. j L. H. Scharpen and V. W. Laurie, J. Chem. Phys., 1965, 43, 2765. ${ }^{k}$ L. Praud, P. Millie, and G. Berthier, Theor. Chim. Acta, 1968, 11, 169. ${ }^{l}$ R. Gunde and A. Ažman, J. Mol. Structure, 1975, 27 , 212.
$s$-triazine ${ }^{7}$ suggest this. The angle for the $N-(2-$ pyridyl) substituent is less easy to decide: it must
reasonably lie between 0 and $30^{\circ}$; we have taken $20^{\circ}$ but alteration in the range $17-25^{\circ}$ does not significantly change the calculated results (reliable experimental data are not available, thus an early paper ${ }^{8}$ suggested 10 $17^{\circ}$ for 2,2 -bipyridyl, and another ${ }^{9}$ coplanarity for 3phenylpyridazine).

Details of the geometry taken for the dipolarophiles are collected in Table 1.

Table 2

| Frontier orbital energies (eV) (CNDO/2) for a series of betaines [cf. (14)] |  |  |  |
| :---: | :---: | :---: | :---: |
| R | $\theta\left({ }^{\circ}\right)$ | $E_{\text {номо }}$ | $E_{\text {Lumo }}$ |
| Me (1) |  | -8.892 | 1.396 |
| H (2) |  | -9.031 | 1.303 |
| Ph (3) | 0.0 | -8.696 | 1.205 |
|  | 23.5 | -8.691 | 1.301 |
|  | 30.0 | -8.688 | 1.355 |
|  | 37.0 | -8.688 | 1.426 |
| 4-Pyridyl (4) | 30.0 | -8.824 | 0.931 |
| 2-Pyridyl (5) | 0.0 | -8.745 | 0.931 |
|  | 6.5 | -8.745 | 0.939 |
|  | 20.0 | -8.743 | 0.999 |
|  | 30.0 | -8.740 | 1.078 |
|  | 35.0 | -8.740 | 1.124 |
|  | 40.0 | -8.740 | 1.176 |
| Pyrimidin-2-yl (6) | 0.0 | -8.699 | 0.950 |
| Triazin-2-yl (7) | 0.0 | -8.789 | 0.708 |
| $\beta$-Formylvinyl (8) | $0.0{ }^{\text {a }}$ | -9.001 | 0.346 |
|  | 180.0 | -8.968 | 0.297 |
| ${ }^{\text {a }}$ As in structure (15). |  |  |  |

HOMO and LUMO Energies for Betaines.-These energies calculated by the $\mathrm{CNDO} / 2$ method are given in Table 2. For the triazinyl and pyrimidinyl substituents we report calculations for a dihedral angle of $0^{\circ}$ only, but for phenyl and 2-pyridyl as substituents we illustrate in
importance of 'HOMO-LUMO' contributions and it is generally agreed that for comparisons within a series


Figure 1 LUMO energies (eV) for betaines as a function of dihedral angle (CNDO/ 2 calculations)
possessing similar transition states, it is the covalent term which varies the most. This has frequently allowed the use of an equation involving such terms alone to interpret successfully experimental results. ${ }^{10}$

Table 3

|  |  | Coefficients (CNDO/2) for betaines |  |  |  |  |  | O |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | C-2 |  |  | 4 | C-6 |  |  |  |
| R | $\theta\left({ }^{\circ}\right)$ | HO | LU | HO | LU | HO | LU | $\stackrel{\text { HO }}{ }$ | LU |
| Me (1) |  | 0.5441 | 0.4746 | 0.3282 | -0.5001 | -0.3678 | 0.4098 | -0.6731 | -0.0085 |
| H (2) |  | 0.5480 | 0.4902 | 0.3271 | $-0.5167$ | $-0.3704$ | 0.4063 | -0.6704 | $-0.0116$ |
| $\mathrm{Ph}(3)$ | 30 | 0.5427 | 0.4244 | 0.3313 | -0.4425 | $-0.3765$ | 0.3734 | -0.6671 | -0.0141 |
| 4-Pyridyl (4) | 30 | 0.5403 | 0.4119 | 0.3306 | -0.4222 | $-0.3688$ | 0.3842 | -0.6729 | $-0.0157$ |
| 2-Pyridyl (5) | 20 | 0.5375 | 0.4192 | 0.3336 | -0.4231 | $-0.3723$ | 0.3872 | -0.6727 | -0.0212 |
| Pyrimidin-2-yl (6) | 0 | 0.5421 | 0.4256 | 0.3295 | -0.4348 | $-0.3673$ | 0.3995 | -0.6738 | -0.0175 |
| Triazin-2-yl (7) | 0 | 0.5439 | 0.4115 | 0.3281 | $-0.4202$ | -0.3659 | 0.3940 | -0.6739 | -0.0169 |
| $\beta$-Formylvinyl (8) | 0 | 0.5504 | 0.3528 | 0.3243 | -0.3716 | $-0.3673$ | 0.3510 | -0.6694 | -0.0071 |

Table 2 and Figure 1 the dependence of the LUMO orbital energies on the dihedral angle taken [whereas the $E(\mathrm{HOMO})$ remains almost constant]. From Figure 1, and the experimental finding that the $N$-phenyl-betaine (3) is more reactive than the $N$-methyl-betaine (1), it follows that the dihedral angle for (3) must be less than $35^{\circ}$. Similarly, as the $N$-(pyrimidin-2-yl)-betaine (6) is more reactive than the $N$-(2-pyridyl)-analogue (5) (and the experimental comparison involves the 5 -nitro-2-pyridyl substituent which is certainly further activated) the dihedral angle for (5) must be above $13^{\circ}$. The values justified previously are in accord with these restrictions. Table 3 records values of orbital coefficients at the positions of interest.

Theoretical Model.-The general method of perturbation applied to interacting systems has indicated the

In Hückel calculations in which electron-electron interactions are not included specifically, the evaluation

(14)

$(15)^{\ddagger}$

(A)

Cf. E. A. Cherniak and C. C. Costain, J. Chem. Phys., 1966, 45, 104. Calculations for the orientation (A) give very similar results and are not separately included.
of the HOMO-LUMO interaction terms is relatively simple; ${ }^{11}$ their evaluation is more complex for SCF methods of the CNDO type. However following Sustmann, ${ }^{12}$ the semiempirical nature of the CNDO
method can justify limiting the contribution of covalent interactions to that given in equation (1) which is limited to interaction between atoms which are becoming directly bonded to each other. We use equation (1) in the present paper: the more negative the values of $\Delta E_{\text {int }}$ the greater the expected stabilisation of the transition state.

In addition, Sustmann ${ }^{12}$ found that in certain data sets the experimental findings were rationalised by

$$
\begin{align*}
& \Delta E_{\mathrm{int}}{ }^{2}=\frac{\left[\left(C_{\mathrm{HO}^{1}} C_{\mathrm{LU}^{1 \prime}}+C_{\mathrm{HO}^{2}} C_{\mathrm{LU}^{2 \prime}}\right) \beta_{r s}\right]^{2}}{E_{\mathrm{HO}}{ }^{\mathrm{A}}-E_{\mathrm{LU}^{3}}{ }^{3}}+ \\
& \frac{\left[\left(C_{\mathrm{HO}^{1}} C_{\mathrm{LU}^{1}}+C_{\mathrm{HO}^{2 \prime}} C_{\mathrm{LU}^{2}}\right) \beta_{r . s}\right]^{2}}{E_{\mathrm{HO}^{B}}{ }^{\mathrm{B}}-E_{\mathrm{LU}^{\mathrm{A}}}}  \tag{1}\\
& \Delta E_{\mathrm{int}}{ }^{2}=K^{2}\left[\frac{1}{E_{\mathrm{HO}^{\mathrm{A}}}-E_{\mathrm{LU}^{\mathrm{B}}}}+\frac{1}{E_{\mathrm{HO}^{B}-E_{\mathrm{LU}}}{ }^{\mathrm{A}}}\right] \tag{2}
\end{align*}
$$

equation (2), which derives from equation (1) if the numerators remain constant. Trong Anh ${ }^{13}$ has justified
neglected in comparison with the second term, thus simplifying equation (3) to the equation (4) utilised in the

$$
\begin{gather*}
\Delta E_{\mathrm{AB}}^{1}=\sum^{\mathrm{A}} \sum_{k}^{\mathrm{B}}\left[q_{l} q_{l} \gamma_{k l}+\left(e^{2} / r_{k l}-\gamma_{k l}\right) Z_{k} Z_{l}\right]  \tag{3}\\
\Delta E_{\text {steric }^{1}}=\sum_{k}^{\mathrm{A}} \sum_{l}^{\mathrm{B}}\left(e^{2} / r_{k l}-\gamma_{k l}\right) Z_{k} Z_{l} \tag{4}
\end{gather*}
$$

present paper. Here, the higher the positive value of $\Delta E_{\text {steric }}$ the less favourable is the transition state.

Dimerisation.-Application of equation (1) indicates (Table 4) that regioisomers of type $2,2^{\prime}-4,6^{\prime}(16)$ should be formed more easily than those of type $4,2^{\prime}-2,6^{\prime}$ (17). This is in complete agreement with the experimental findings for the 2 -pyridyl (5) and the triazin- 2 -yl betaines (7) ${ }^{17}$ for which only dimers of type (16a) are formed. ${ }^{2}$ The pyrimidin-2-yl-betaine (6) ${ }^{2}$ forms the dimer of type (16a) by kinetic control although equili-

## Table 4

Transision-state energies [energies in a.u.; 1 a.u. $=4.3598 \times 10^{-18} \mathrm{~J}$; however energies calculated by formulae (1), (2), and (4) are not directly comparable] for thermal dimerisation of 1 -substituted 3 -oxidopyridiniums

| Eqn.(1) | Isomer |  | $\underset{(1)}{\mathrm{Me}}$ | $\begin{gathered} \mathrm{Ph}(3) \\ \left(\theta=30^{\circ}\right) \end{gathered}$ | 4-Pyridyl <br> (4) $\left(\theta=30^{\circ}\right)$ | 2-Pyridyl <br> (5) $\left(\theta=20^{\circ}\right.$ | Pyrimidin- <br> (6) $\left(\theta=0^{\circ}\right)$ | Triazin-2-yl <br> (7) $\left(\theta=0^{\circ}\right)$ | $\beta$-Formylvinyl <br> (8) $\left(\theta=0^{\circ}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | orientation | structure |  |  |  |  |  |  |  |
|  | $\left\{2,2^{\prime}-4,6^{\prime}\right.$ | (16) | -0.0528 | -0.0438 | -0.0423 | -0.0436 | -0.0457 | $-0.0437$ | -0.0340 |
|  | $\left\{2,6^{\prime}-4,2^{\prime}\right.$ | (17) | -0.0518 | $-0.0430$ | $-0.0418$ | $-0.0430$ | $-0.0453$ | $-0.0435$ | $-0.0343$ |
| (2) | $\left\{\begin{array}{l}2,2^{\prime}-4,6^{\prime} \\ 2,6^{\prime}-4,2^{\prime}\end{array}\right.$ | (16) | -5.29 | -5.42 | $-5.58$ | -5.61 | -5.64 | $-5.73$ | $-5.82$ |
|  |  | \{ 16 a ) | 5.21 | 8.58 | 8.51 | 8.42 | 8.47 | 8.42 | 6.85 |
| (4) | 2,2-4,6 | $\{$ (16b) | 5.57 | 8.14 | 8.09 | 7.94 | 7.90 | 7.88 | 6.77 |
|  | 2,6'-4, $\mathbf{2}^{\prime}$ | $\{(17 a)$ | 5.21 | 10.21 | 10.04 | 10.17 | 8.63 | 8.57 | 6.59 |
|  |  | (17b) | 5.44 | 7.85 | 7.79 | 7.87 | 7.59 | 7.57 | 6.51 |
| Exp. \% |  |  | (none) | (none) | (none) | 100\% (16a) | 100\% (16a) | 100\% (16a) | $100 \%$ (16a) |

${ }^{a}$ Ref. 2. ${ }^{b}$ The equilibrium value is $67 \% 2,6^{\prime}-4,2^{\prime}(17 \mathrm{a})$ and $33 \% 2,2^{\prime}-4,6^{\prime}(16 \mathrm{a}) .{ }^{c}$ Ref. 17 . ${ }^{d}$ A. R. Katritzky, N. Dennis, G. W. Fischer, S. Rahimi-Rastgoo, and G. J. Sabongi, unpublished results.
this model by the hypothesis that the distance between the reactants in a series of transition states is itself proportional to the product of the coefficients of the frontier orbitals. As the integrals $\beta_{r s}$ are proportional to the overlap, i.e. inversely proportional to the distance, then terms of type $\left(C_{\text {HO }} C_{\mathrm{LU}} \boldsymbol{\beta}_{r s}\right)$ become invariant. We have also used equation (2) in the present paper: as with equation (1) the more negative the value of $\Delta E_{\text {int }}$ the greater the expected stabilisation of the transition state.

If the second-order perturbational treatment is limited to the principal frontier orbital interactions [equations (1) and (2)], it is obviously impossible to differentiate between the formation of exo- and endostereochemical isomers. The inclusion of the so-called secondary interactions as suggested by Woodward and Hoffman is not always sufficient to explain the observed orientation. ${ }^{14}$ Sustmann ${ }^{15}$ has shown that the orientation of addition of cyclopropene to cyclopentadiene could be correlated by using first-order interaction terms corrected by including repulsion terms of the type proposed by Dewar ${ }^{16}$ and adopted in the MINDO/2 treatment. The expression for such interaction terms of the first order is given by equation (3); however, for species not bearing high charges, the first term can be
bration via dedimerisation gives considerable amounts of (17a) by thermodynamic control.

$2,2^{\prime} 4,6^{\prime}$
(16a)

$4,2^{\prime} 2,6^{\prime}$
(17a)


4, $2^{\prime} 2,6^{\prime}$
(17b)

However equation (1) cannot explain the relative ease of dimerisation in this series: we find experimentally

* $\gamma_{k l}$ is the distance between centre $s k$ and $l ; \gamma_{k l}$ is the exchange integral, calculated empirically following the method of K. Ohno, Theor. Chim. Acta, 1964, 2, 219; $Z_{k}$ is the charge on atom $k$.
zero tendency for the $N$-methyl (1), $N$-phenyl (3), and 4-pyridyl (4) compounds with dimerisation rate increasing for $(5) \sim(8)<(6)<(7)$. Equation (1) would


Figure 2 Plot of $\log k+6$ against transition state energy, as calculated by equation (2), for addition of methyl acrylate to a series of 1 -substituted 3 -oxidopyridiniums
suggest rates of $(1) \gg(6)>(3) \sim(7) \sim(5)$, a completely different order. Equation (2) gives the order
formation indeed varies in the way previously discussed; i.e., that the distance between the reactive species in the transition state for dimer formation is related to the orbital coefficients on the atoms becoming linked.

We have utilised equation (4) in an attempt to rationalise the stereochemistry of the addition. However, in each case the steric term should favour endo-addition in place of the exo-process exclusively found. We believe that steric hindrance between remote parts of the molecules intervenes to disfavour endo-attack; this hypothesis is supported by the examination of models.

Reactions of Methyl Acrylate with a Series of Betaines.The data are set out in Table 5. Again equation (1) indicates that regioisomers of type (18) should be preferred in all cases-in complete agreement with experiment. Again the relative rates which are found to increase for $(1) \ll(3) \ll(6)$ cannot be explained by treatment using equation (1) [which predicts $(1)>(6) \sim(3)]$ but are fully explained by treatment using equation (2) which indicates $(1) \ll(3) \ll(5)<(6)<(7)$. The log $k$ values (Table 5) show a fair linear relation with the total $E_{\text {int }}$ calculated by equation (2) (Figure 2). The data for 2 -pyridyl are too high for the monotonic relation expected; we ascribe this to the use of the 5 -nitro-2-pyridyl substituent in the kinetic work; the points for phenyl, pyrimidin-2-yl, and 4-pyridyl are precisely linear.

Analysis into the individual HOMO (betaine)-LUMO (dipolarophile) $\left(\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}\right)$ and LUMO (betaine)-HOMO (dipolarophile) $\left(\mathrm{L}_{B} \mathrm{H}_{\mathrm{D}}\right)$ contributions to the total energy term (see Table 5) shows that [using the treatment of equation (2)] the increased reactivity of the phenyl compound over the methyl and hydrogen analogue

Table 5
Transition-state energies (a.u.) for addition of methyl acrylate to a series of 1 -substituted 3 -oxidopyridiniums

| Eqn. | Me (1) | H (2) | $\mathrm{Ph}(3)$ $\left(\theta=30^{\circ}\right)$ | $\begin{gathered} \text { 4-Pyridyl } \\ (4) \\ \left(\theta=30^{\circ}\right) \end{gathered}$ | $\begin{aligned} & \text { 2-Pyridyl } \\ & \begin{array}{l} (5) \\ \left(\theta=20^{\circ}\right) \end{array} \end{aligned}$ | $\begin{gathered} \text { Pyrimidin- } \\ 2-\mathrm{yl} \\ (6) \\ \left(\theta=0^{\circ}\right) \end{gathered}$ | $\begin{gathered} \text { Triazin- } \\ 2-\mathrm{yl} \\ (7) \\ \left(\theta=0^{\circ}\right) \end{gathered}$ | $\begin{gathered} \beta \text {-Formyl- } \\ \text { vinyl } \\ (8) \\ \left(\theta=0^{\circ}\right) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (1) $\quad \mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | -0.0332 | -0.0333 | -0.0342 | $-0.0332$ | -0.0335 | -0.0336 | -0.0334 | -0.0335 |
| (18) $\left\{\mathrm{L}_{\mathbf{B}} \mathrm{H}_{\mathrm{D}}\right.$ | -0.0098 | -0.0101 | $-0.0079$ | $-0.0080$ | -0.0080 | $-0.0087$ | -0.0084 | -0.0065 |
| Total | -0.0430 | -0.0434 | -0.0422 | -0.0413 | -0.0418 | -0.0423 | -0.0418 | -0.0400 |
| $\left(\mathrm{H}_{\mathrm{B}} \mathrm{L}_{1}\right.$ | -0.0285 | -0.0287 | -0.0298 | $-0.0287$ | -0.0291 | -0.0290 | -0.0287 | -0.0287 |
| (19) $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{1}\right.$ | -0.0094 | -0.0097 | $-0.0077$ | $-0.0079$ | -0.0081 | -0.0085 | -0.0083 | -0.0065 |
| Total | -0.0379 | -0.0384 | -0.0375 | $-0.0366$ | -0.0372 | -0.0375 | -0.0370 | -0.0352 |
| (2) $\quad \mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | -2.40 | $-2.37$ | $-2.45$ | -2.42 | -2.44 | -2.45 | $-2.43$ | -2.38 |
| $(18,19) \quad\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ | $-1.78$ | -1.79 | -1.78 | $-1.83$ | $-1.83$ | $-1.83$ | $-1.86$ | -1.91 |
| Total | -4.18 | -4.16 | -4.23 | -4.25 | -4.27 | -4.28 | $-4.29$ | -4.29 |
| (4) (18b) exo | 3.66 | 2.88 | 6.16 | 6.50 | 6.07 | 5.43 | 5.42 | 4.43 |
| (18a) endo | 5.64 | 3.51 | 4.54 | 4.81 | 4.72 | 4.47 | 4.47 | 4.16 |
| (19b) exo | 5.30 | 2.91 | 5.22 | 5.30 | 5.14 | 5.29 | 5.27 | 4.73 |
| (19a) endo | 4.08 | 3.72 | 4.69 | 4.68 | 4.60 | 4.64 | 4.64 | 4.37 |
| Exp. \% (18b) | $50{ }^{a}$ | $50{ }^{\text {b }}$ | $37{ }^{\circ}$ | $0{ }^{\text {d }}$ | $75{ }^{\text {c }}$ | $42{ }^{f}$ | $60{ }^{g}$ | $60{ }^{h}$ |
| (18a) | 50 | 50 | 63 | 100 | 25 | 58 | 40 | 40 |
| Exp. $\log k+6$ | $0.56{ }^{\text {i }}$ |  | $1.07{ }^{i}$ | $1.90{ }^{j}$ | $3.12{ }^{\text {j }}$ | $3.08{ }^{i}$ |  |  |

${ }^{a}$ A. R. Katritzky and Y. Takeuchi, $J$. Chem. Soc. (C), 1971, 874. b J. Banerji, N. Dennis, J. Frank, A. R. Katritzky, and T. Matsuo, J.C.S. Perkin I, 1976, 2334. ${ }^{c}$ (i) N. Dennis, A. R. Katritzky, T. Matsuo, S. K. Parton, and Y. Takeuchi, J.C.S. Perkin I, 1974, 746 ; (ii) N. Dennis, A. R. Katritzky, S. K. Parton, Y. Nomura, Y. Takahashi, and Y. Takeuchi, J.C.S. Perkin I, $1976,2289$. ${ }^{d}$ A. R. Katritzky, J. Banerji, A. Boonyarakvanich, A. Cutler, N. Dennis, S. Q. A. Rizvi, Gr. J. Sabongi, and H. Wilde, preceding paper. ${ }^{e}$ Ref. 3. ${ }^{f}$ Ref. 20. ${ }^{g}$ Ref. 17. ${ }^{h}$ Table 4 footnote $d .{ }^{i}$ Rate constants at $54{ }^{\circ} \mathrm{C}$ calculated from variable temperature kinetic data in ref. 4. ${ }^{j}$ Measured at $54{ }^{\circ} \mathrm{C}$, unpublished results with B. El-Osta, G. Musumarra, and C. Ögretir.
$(1)<(3)<(4)<(5)<(6)<(7)$ in complete agreement with experiment (Table 4). This result indicates that the structure of the transition state for dimer
depends on increase in $H_{B} L_{D}$. However the reactivity sequence $(3) \ll(5)<(6)<(7)$ is dominated by increasing $\mathrm{L}_{B} \mathrm{H}_{\mathrm{D}}$ contributions whilst $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ remains
almost constant. This is of course as expected: the energy of $\mathrm{H}_{\mathrm{B}}$ increases with increasing conjugation, but

increasing numbers of heteroatoms decrease the $\mathrm{L}_{\mathrm{B}}$ value leaving $\mathrm{H}_{\mathrm{B}}$ little affected.
(EtOCH: $\mathrm{CH}_{2}$ ) again Table 6 data predict preferred regioisomers (18) for all betaines in complete agreement with experiment. Again the relative rates, which from qualitative preparative work we know to increase in the same manner as those for methyl acrylate, cannot be explained by equation (1), but are rationalised by treatment using equation (2). The incomplete quantitative rate data once again indicate too high a value for 2-pyridyl: the discrepancy is greater than previously discussed for the acrylate addition, in good agreement with the supposition that it is the 5 -nitro-group which should enhance the addition with the electron-rich olefin more than for the electron-deficient acrylate.

Table 6
Transition state energies (a.u.) for addition of ethyl vinyl ether to a series of 1 -substituted 3 -oxidopyridiniums

|  |  | Ph (3) | 4-Pyridyl <br> (4) | 2-Pyridyl <br> (5) | $\begin{gathered} \text { Pyrimidin- } \\ 2-\mathrm{yl} \end{gathered}$ <br> (6) | Triazin-2-yl <br> (7) | $\beta$-Formylvinyl <br> (8) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Eqn. <br> (1) | Structure | ( $\theta=30^{\circ}$ ) | $\left(\theta=30^{\circ}\right)$ | $\left(0=20^{\circ}\right)$ | $\left(\theta=0^{\circ}\right)$ | $\left(0=0^{\circ}\right)$ | $\left(\theta=0^{\circ}\right)$ |
|  | (18) | $-0.0482$ | -0.0472 | -0.0479 | -0.0486 | $-0.0479$ | -0.0447 |
|  | (19) | -0.0462 | -0.0457 | -0.0463 | -0.0470 | -0.0464 | -0.0435 |
| (2) |  | -3.95 | -3.99 | $-4.00$ | -4.01 | $-4.03$ | $-4.06$ |
| (4) | (18b) exo | 5.42 | 6.69 | 5.46 | 4.81 | 4.79 | 3.94 |
|  | (18a) endo | 3.69 | 3.76 | 3.64 | 3.63 | 3.62 | 3.33 |
|  | (19b) exo | 3.87 | 3.95 | 3.78 | 3.89 | 3.88 | 3.56 |
|  | (19a) endo | 4.78 | 4.89 | 4.34 | 4.75 | 4.74 | 4.48 |
| Exp. \% |  | $a$ | 100\% (18a) ${ }^{\text {b }}$ | 100\% (18a) ${ }^{\text {c }}$ | $100 \%(18 \mathrm{a})^{d}$ | 100\% (18a) ${ }^{\circ}$ | 100\% (18a) ${ }^{\text {c }}$ |
| Exp. | $\log k+5$ |  | $0.16{ }^{f}$ | $1.55{ }^{f}$ | $1.10^{f}$ |  |  |

${ }^{\bullet}$ No reaction. ${ }^{\boldsymbol{b}}$ A. R. Katritzky, A. Boonyarakvanich, N. Dennis, and G. J. Sabongi, unpublished results. ${ }^{\circ}$ Ref. 3. ${ }^{\text {d }}$ Ref. 20. - Table 5, footnote $h$. ${ }^{f}$ Table 5, footnote $j$. ${ }^{g}$ A. R. Katritzky, M. Abdullah, S. Bayyuk, A. M. A. Bolouri, N. Dennis, and G. J. Sabongi, in preparation.

Treatment by equation (4) indicates that for the methyl (1) and hydrogen compounds (2) exo-products should be favoured but that the aryl substituents should

Finally, in every case endo is predicted and in every case endo is found.

Reaction of Styrene with a Series of Betaines.-The

Table 7
Transition-state energies (a.u.) for addition of styrene to a series of 1 -substituted 3 -oxidopyridiniums

| Eqn. <br> (l) | Structure | Energy | Ph (3) | 4-Pyridyl <br> (4) | 2-Pyridyl <br> (5) | $\begin{gathered} \text { Pyrimidin- } \\ 2-y l \end{gathered}$ <br> (6) | $\begin{gathered} \text { Triazin- } \\ 2-\mathrm{yl} \end{gathered}$ <br> (7) | $\beta$-Formylvinyl <br> (8) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | separation | $\left(0=30^{\circ}\right.$ ) | $\left(0=30^{\circ}\right)$ | $\left(\theta=20^{\circ}\right)$ | $\left(\theta=0^{\circ}\right)$ | $\left(\theta=0^{\circ}\right)$ | $\left(\theta=0^{\circ}\right)$ |
|  | (18) | $\int \mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | $-0.0183$ | -0.0178 | -0.0179 | -0.0180 | -0.0179 | -0.0179 |
|  |  | $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ | -0.0115 | -0.0116 | -0.0119 | -0.0124 | -0.0120 | -0.0094 |
|  |  | Total | -0.0298 | -0.0294 | -0.0298 | -0.0304 | -0.0299 | -0.0273 |
|  | (19) | $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | -0.0161 | -0.0155 | -0.0158 | -0.0157 | -0.0156 | -0.0155 |
|  |  | $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ | -0.0109 | -0.0113 | -0.0115 | -0.0121 | -0.0118 | -0.0094 |
|  |  | Total | -0.0270 | -0.0268 | -0.0273 | -0.0278 | -0.0274 | -0.0249 |
| (2) | $(18,19)$ | $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | -2.34 | $-2.32$ | $-2.34$ | $-2.34$ | -2.32 | $-2.28$ |
|  |  | $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ | $-1.98$ | $-2.04$ | $-2.03$ | -2.04 | $-2.08$ | $-2.14$ |
|  |  | Total | $-4.32$ | $-4.36$ | $-4.37$ | $-4.38$ | $-4.40$ | -4.42 |
| (4) | (18b) | exo | 6.76 | 7.91 | 6.74 | 5.97 | 5.94 | 4.77 |
|  | (18a) | endo | 4.97 | 5.23 | 5.17 | 4.89 | 4.88 | 4.52 |
|  | (19b) | exo | 5.71 | 5.75 | 5.56 | 5.81 | 5.79 | 5.25 |
|  | (19a) | endo | 5.25 | 5.37 | 5.02 | 5.21 | 5.20 | 4.92 |
| Exp. \% |  |  | 100\% (18a) ${ }^{\text {a }}$ | 100\% (18a) ${ }^{\text {b }}$ | $\begin{gathered} 92 \%(18 a)^{c} \\ 8 \%(18 b) \end{gathered}$ | 100\% (18a) ${ }^{\text {c }}$ | 100\% (18a) ${ }^{\text {d }}$ | 100\% (18a) |
| Exp. |  | $\log k+5$ |  | $0.30{ }^{f}$ | $1.65{ }^{f}$ | $1.33{ }^{f}$ |  |  |

afford more endo-addition. Experimentally from the crude and approximate data presently available there is some support for this: whereas the H and the Me substituents both yield about equal amounts of endo- and exo-conformers, some of the aryl substituents (phenyl and 4-pyridyl) give a predominance of endo.

Reactions of Ethyl Vinyl Ether with a Series of Betaines. -For the representative electron-rich dipolarophile
position described in Table 7 for the conjugated dipolarophile styrene is very similar to that just described for ethyl vinyl ether: regioisomers (18) are predicted by equation (1), relative rates explained by equation (2), except for the influence of the 5-nitro-group in 2-pyridyl, and endo-isomers correctly predicted by equation (4).

Reactions of 1-(Pyrimidin-2-yl)-3-oxidopyridinium with a Series of Olefinic Dipolarophiles.-These data are
collected in Table 8. We now find that equation (1) indicates correctly that regioisomers of type (18) should be preferred for all the monosubstituted ethylenes $\mathrm{CH}_{2}=\mathrm{CHR}$ with $\mathrm{R}=\mathrm{OEt}, \mathrm{CN}, \mathrm{CO}_{2} \mathrm{Me}, \mathrm{Ph}$, and 4pyridyl.

Experimentally, $\mathrm{CH}_{2}=\mathrm{CHOEt}$ gives mainly one endocompound [cf. (18a)] whereas the other olefins give comparable amounts of the two stereoisomers [cf. (18a) and (18b)]. The steric terms obtained by the treatment

For vinyl acetate a second MO of type $\pi$ near to the LUMO characterised by coefficients of considerably greater amplitude on carbon atoms $\mathrm{C}-1$ and $\mathrm{C}-2$ :

$$
\begin{aligned}
& \varepsilon_{\text {LUMO }}=0.1618 \text { a.u. C-1 } 0.2927 \text { C-2 }-0.2958 \\
& \varepsilon_{\text {SUMO }}=0.2022 \text { a.u. C-1 } 0.6598 \text { C-2 }-0.5978
\end{aligned}
$$

The treatment in Table 9 indicates that the interaction $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ is far less than $\mathrm{H}_{\mathrm{B}} \mathrm{S}_{\mathrm{D}}$. The total interaction is therefore calculated using $\mathrm{S}_{\mathrm{D}}$ in place of $\mathrm{L}_{\mathrm{D}}$.*

Table 8
Transition state interaction energies (a.u.) for addition of 1-(pyrimidin-2-yl)-3-oxidopyridinium to a series of monosubstituted olefinic dipolarophiles $\mathrm{CH}_{2} \cdot \mathrm{CH} \cdot \mathrm{X}$

| Eqn. <br> (1) | Structure |  | $\mathrm{CH}_{2} \mathrm{OH}$ | Cyclohexene | $\mathrm{OBu}{ }^{\text {n }}$ | OEt | Ph | CN | 4-Pyridyl | $\mathrm{CO}_{2} \mathrm{Me}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (18) | $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | $-0.0403$ | -0.0357 | -0.0341 | -0.0335 | -0.0180 | -0.0405 | -0.0175 | $-0.0336$ |
|  |  | $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ | -0.0156 | -0.0220 | -0.0143 | -0.0151 | -0.0124 | -0.0216 | -0.0128 | $-0.0087$ |
|  |  | Total | -0.0559 | $-0.0577$ | -0.0484 | -0.0486 | -0.0304 | -0.0621 | $-0.0303$ | -0.0423 |
|  | (19) | $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | $-0.0397$ |  | -0.0330 | -0.0325 | -0.0157 | -0.0377 | $-0.0150$ | -0.0289 |
|  |  | $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ | $-0.0153$ |  | -0.0138 | -0.0145 | -0.0121 | -0.0213 | $-0.0125$ | -0.0085 |
|  |  | Total | $-0.0550$ |  | -0.0468 | -0.0470 | -0.0278 | -0.0590 | -0.0275 | -0.0374 |
| (2) | $(18,19)$ | $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | -2.02 | -2.06 | -2.01 | -2.01 | -2.34 | -2.29 | -2.42 | $-2.45$ |
|  |  | $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ | $-1.85$ | $-1.66$ | $-2.00$ | $-2.00$ | -2.04 | $-1.80$ | $-1.97$ | $-1.83$ |
|  |  | Total | $-3.88$ | $-4.02$ | -4.02 | -4.01 | -4.38 | -4.09 | -4.39 | -4.28 |
| (4) | (18b) | exo | 3.86 | 5.44 | 5.59 | 4.81 | 5.97 | 3.51 | 5.94 | 5.43 |
|  | (18a) | endo | 3.62 | 6.59 | 3.98 | 3.63 | 4.89 | 3.25 | 4.87 | 4.47 |
|  | (19b) | exo | 3.82 |  | 4.34 | 3.89 | 5.81 | 3.46 | 5.79 | 5.29 |
|  | (19a) | endo | 3.78 |  | 5.45 | 4.75 | 5.21 | 3.38 | 5.19 | 4.64 |
| Exp. \% |  |  | $\begin{gathered} 100 \% \\ (18 \mathrm{a})^{a} \end{gathered}$ | $\begin{gathered} 100 \% \\ (18 \mathrm{a})^{a} \end{gathered}$ |  | $\begin{gathered} 100 \% \\ (18 \mathrm{a})^{a} \end{gathered}$ | $\begin{aligned} & 100 \% \\ & (18 a)^{b} \end{aligned}$ | $\begin{gathered} 84 \% \\ (18 a)^{a} \end{gathered}$ | $a$ | $\begin{gathered} 58 \% \\ (18 a)^{a} \end{gathered}$ |
|  |  |  |  |  |  |  |  | $16 \%$ |  | $42 \%$ |
| Exp. | $\log k+7$ |  | $0.87{ }^{\text {c }}$ | $1.97{ }^{\circ}$ | $2.75{ }^{\text {d }}$ |  | $2.96{ }^{\text {d }}$ | $3.10{ }^{\text {d }}$ | $3.20{ }^{\text {d }}$ | $3.651{ }^{\text {d }}$ |

${ }^{a}$ Ref. 20. ${ }^{b}$ Ref. 3. ${ }^{c}$ Extrapolated from variable temperature measurements to $42{ }^{\circ} \mathrm{C}$; unpublished results with B . El-Osta, G. Musumarra, and C. Öḡretir. ${ }^{d}$ Ref. 4, measured at $42{ }^{\circ} \mathrm{C}$.
using equation (4) favour the endo-product for all the additions to give regioisomer (18), the difference is the greatest for ethyl vinyl ether and least for acrylonitrile.

Again the treatment using equation (1) does not reproduce the experimental kinetic results which indicate increasing rates of reaction for the vinyl compounds in the order: $\mathrm{OBu}^{\mathrm{n}}<\mathrm{Ph}<\mathrm{CN}<4$-pyridyl $<\mathrm{CO}_{2} \mathrm{Me}$. However equation (2) does explain the relative rates, provided that styrene and 4 -vinylpyridine (which were taken as planar for the calculations) are considered separately from the others.

Table 8 also gives a comparison of the results by the treatment using equation (2) for this wide variety of olefinic dipolarophiles with the kinetic second-order rate constants for reaction at $42{ }^{\circ} \mathrm{C} .{ }^{4}$ Figure 3 shows that there is a general trend to increasing rates as $\Delta E$ increases, but that there is no precise relationship between $\log k$ and $\Delta E$.

Such a correlation provides evidence for the model including only the frontier interactions [equation (2)]: no correlation is found with the treatment of equation (1) which involves also the coefficients at the various interaction atoms.

It is further evident from Table 8 that the HOMO (betaine)-LUMO (dipole) interaction is dominating the variation in reactivity. For the planar $\mathrm{CH}_{2}=\mathrm{CHX}$ series, a linear correlation (correlation coefficient 0.954 ) is obtained for a plot of $\log k$ against $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$, but no significant correlation is found between $\log k$ and $\mathrm{H}_{\mathrm{D}} \mathrm{L}_{\mathrm{B}}$.

Site Selectivity of Monoenes.-Cycloaddition of 3oxidopyridinium and dienes can obviously occur at

Table 9
Transition state energies (a.u.) for addition of s-trans- and $s$-cis-vinyl acetate to 1 -(pyrimidin-2-yl)-3-oxidopyridinium ${ }^{a}$


Exp. \% 100\% (18a) ${ }^{b}$
${ }^{a}$ Primed numbers refer to vinyl acetate. $\mathrm{C}-\mathbf{1}^{\prime}$ is attached to the oxygen atom. ${ }^{b}$ Ref. 20.
several sites. However such site selectivity is also possible for monoenes: besides addition at 2,6 (and the

* It must be noted that the use of solely the $S_{D}$ in place of $L_{D}$ would indicate formation of the $\beta$-regioisomer: however the differences in $E_{\text {int }}$ for the $\alpha$ - and $\beta$-isomers is small. Experimentally we found only the $\alpha$-isomer.
forbidden addition at 2,4 ) reaction is allowed at the $\mathrm{O}, 2[\longrightarrow(20)]$ or $\mathrm{O}, 4$ positions $[\longrightarrow(21)]$. Experi-

(19a)

(19b)
mentally such addition modes have been involved in the reactions of $\alpha$-halogenoketens with the betaines [when spontaneous elimination of hydrogen halide yields
most $2 \pi$-addends) addition at 0,2 or 0,4 does not lead to a stable product. For difluoroketen, the same


Figure 3 Correlation of FMO energies [equation (2)] with rate constants for additions to 1-(4,6-dimethylpyrimidin-2-yl-) 3 -oxidopyridinium: I, corr. coeff. 0.997 ; II, corr. coeff. 0.942
products of type (22) ${ }^{18}$ and (23) ${ }^{19}$ ]. We have calculated (Table 10) energy terms for various orientations of addition.

(21)

(22)

(23)
pattern emerges, but now orientation of addition of type $(24 \alpha)$ or $(25 \alpha)$ can lead to stable products by elimin-

Figure 3 Correlation of FMO energies [equation (2)] with rate constants for additions to 1 -(4,6-dimethylpyrimidin-2-yl-)
ation of HF. Experimentally dichloroketen does add across the 0,4 positions ${ }^{18}$ while aryl(chloro) ketens react at both the $\mathrm{O}, 2$ and $\mathrm{O}, 4$ positions. ${ }^{19}$

Table 10
Site selectivity for the cycloaddition of acrylonitrile, difluoroketen, and keten to 1-methyl-3-oxidopyridinium

|  |  | $\stackrel{2^{\prime}}{\mathrm{CH}_{2}}=\stackrel{1^{\prime}}{\mathrm{CH}}-\mathrm{CN}$ |  |  | $\stackrel{2^{\prime}}{\mathrm{CF}_{2}=} \stackrel{1}{\mathrm{C}}^{\prime}=\mathrm{O}$ |  |  | $\begin{gathered} 2^{\prime} \quad 1^{\prime} \\ \mathrm{CH}_{2}=\mathrm{C}=\mathrm{O} \end{gathered}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{gathered} 2,6 \\ (18) \text { or }(19) \end{gathered}$ | $\begin{aligned} & \mathrm{O}, 2^{a} \\ & (25) \end{aligned}$ | $\begin{gathered} \mathrm{O}, 4^{b} \\ (24) \end{gathered}$ | $\begin{gathered} 2,6 \\ (18) \text { or }(19) \end{gathered}$ | $\begin{aligned} & \mathrm{O}, 2^{a} \\ & (25) \end{aligned}$ | $\begin{gathered} \mathrm{O}, 4^{b} \\ (24) \end{gathered}$ | $\begin{gathered} 2,6^{c} \\ (18) \text { or }(19) \end{gathered}$ | $\mathrm{O}, 2^{d}$ <br> (25) | $\begin{aligned} & \mathrm{O}, 4^{e} \\ & (24) \end{aligned}$ |
| (1) | $\int \mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}$ | -0.0401 | -0.0689 | -0.0447 | $-0.0396$ | -0.0750 | -0.0523 | -0.0389 | -0.0651 | $-0.0413$ |
|  | $\alpha<\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}$ | -0.0242 | -0.0084 | -0.0095 | $-0.0234$ | -0.0092 | -0.0103 | $-0.0209$ | $-0.0020$ | -0.0025 |
|  | Total | $-0.0643$ | $-0.0773$ | -0.0542 | $-0.0630$ | -0.0842 | -0.0626 | $-0.0598$ | $-0.0671$ | $-0.0438$ |
|  | $\left(\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{D}}\right.$ | -0.0373 | -0.0718 | -0.0509 | -0.0415 | $-0.0730$ | -0.0482 | $-0.0350$ | -0.0692 | -0.0499 |
|  | $\beta<\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}$ | -0.0236 | $-0.0057$ | -0.0066 | $-0.0222$ | -0.0046 | -0.0054 | -0.0237 | -0.0136 | -0.0149 |
|  | Total | $-0.0609$ | $-0.0775$ | -0.0575 | $-0.0637$ | -0.0776 | -0.0536 | -0.0587 | -0.0828 | -0.0648 |
| (2) | $\int \mathrm{H}_{B} \mathrm{~L}_{\mathrm{D}}$ |  | -2.26 |  |  | -1.99 |  |  | -1.82 |  |
|  | $\left\{\mathrm{L}_{\mathrm{B}} \mathrm{H}_{\mathrm{D}}\right.$ |  | $-1.75$ |  |  | -1.99 |  |  | -1.94 |  |
|  | Total |  | -4.00 |  |  | -3.98 |  |  | -3.76 |  |
| (4) | $\alpha\{$ exo | 2.65 | 2.68 | 2.37 | 3.23 | 2.92 | 2.81 | 2.21 | 2.07 | 1.96 |
|  | $\alpha$ endo | 2.76 | 3.07 | 2.08 |  |  |  |  |  |  |
|  | $\beta$ exo | 2.66 | 2.64 | 2.81 | 3.18 | 2.79 | 2.69 | 2.23 | 1.87 | 1.83 |
|  | $\beta$ lendo | 2.88 | 2.93 | 2.17 |  |  |  |  |  |  |

${ }^{a}$ Isomers $\alpha=\mathrm{O}, 1^{\prime}-2,2^{\prime}, \quad \beta=\mathrm{O}, 2^{\prime}-2,1^{\prime} . \quad{ }^{b}$ Isomers $\alpha=\mathrm{O}, 1^{\prime}-4,2^{\prime}, \quad \beta=\mathrm{O}, 2^{\prime}-4,1^{\prime}, \quad$ Isomers $\quad \alpha=2,2^{\prime}-6,1^{\prime}, \quad \beta=2,1^{\prime}-6,2^{\prime}$.
${ }^{d}$ Isomers $\alpha=2,1^{\prime}-\mathrm{O}, 2^{\prime}, \beta=2,2^{\prime}-\mathrm{O}, 1^{\prime}$. ${ }^{e}$ Isomers $\alpha=4,1^{\prime}-\mathrm{O}, 2^{\prime}, \beta=4,2^{\prime}-\mathrm{O}, 1^{\prime}$.

For acrylonitrile, the FO term favours addition across the 0,2 positions, while the steric term favours the 0,4 orientation. We believe that the observed 2,6 -addition arises from the fact that for acrylonitrile (and indeed

Site Selectivity of Dienes.-Dienes undergo permitted cycloaddition at either the 2,6 (acting as conjugated monoenes) or 2,4 positions (acting as dienes). Calculations for trans-penta-1,3-diene are given in Table 11.

Of the twelve possible products, eight from addition at 2,6 [endo- and exo-forms of (18), (19), (26), and (27)]



(24)


$\beta$
(25)
and four from addition at 2,4 [endo- and exo-forms of (28) and (29)] we find experimentally only the three endo-forms (18a), (28a), and (29a).

For addition at the 2,4-positions rather similar steric terms and more favourable covalent terms are found. Addition is predicted to be exo; although the endo product is found experimentally, this is believed to be a result of ring inversion after the addition (see later).

For buta-1,3-diene the calculated data are given in Table 12. Here the steric term favours 2,4-addition, and the only product isolated from the reaction mixture ${ }^{20}$ was indeed the endo-2,4-adduct. Again the endoorientation is considered to arise from ring inversion of an initially formed exo-adduct. ${ }^{3}$

Table 13 treats comparable data for cyclopentadiene. The two products isolated experimentally are precisely those expected to be favoured for the 2,4 and for the 2,6 addition modes. Moreover, we can explain the

Table 11
Transition-state interaction energies (a.u.) for the addition of trans-penta-1,3-diene (31) to 1-(pyrimidin-
2-yl)-3-oxidopyridinium
Reaction at 2,6-positions of betaine
Reaction at 2,4-position

| $\overbrace{(26)}^{s-t r a n s-c e n t r a l ~ o l e f i n ~}$ | $(27)$ |
| :---: | :---: |
| -0.0461 | -0.0436 |
| 4.49 | 4.66 |
| 4.67 | 4.54 |


| $\overbrace{(28)}$ | $(29)$ |
| :--- | :--- |
| -0.0515 | -0.0523 |
| 4.61 | 3.87 |
| 4.24 | 3.80 |
| $67 \%[(28 a)$ | $+(29 \mathrm{a})]$ |

${ }^{a}$ Ref. 3.

For addition at the 2,6 -positions the steric factors considerably favour forms (18) and (19) over (26) and
comparable amounts which are formed: the exo-2,4addition product is considerably favoured by the steric

(26a)

(26b)

(27a)

(27b)

(28a)

(28b)

(29a)

(29b)

(30) $R=H$
(31) $R=M e$
(27) and, although the covalent terms act in the opposite direction, the steric effects clearly dominate. Considering only the two forms (18) and (19), the former is favoured both by steric and covalent effects, and indeed the endo-form (18a) is correctly predicted as the preferred product.
term and the endo-2,6- by the covalent term. Here no ring inversion is possible for the exo-2,4-adduct, which consequently is isolated as such and not as the endostereoisomer (as for the acyclic pentadiene analogue).

Site and Regioselectivity of Fulvene Cycloadditions.This is a complex problem. exo- and endo-Additions at

Transition state interaction energies (a.u.) for the addition of buta-1,3-diene (30) to 1-(pyrimidin-2-yl)-3-oxidopyridinium Reaction at 2,6 -position of betaine

| Eqn. |  | s-trans-Olefin |  | $s$-cis-Olefin |  | Reaction at 2,4-position $s$-cis-Diene |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (18) | (19) | (18) | (19) |  |
| (1) |  | -0.0445 | -0.0415 | -0.0434 | -0.0407 | -0.0550 |
| (4) | \{endo | 3.46 | 3.60 | 3.61 | 3.71 | 3.77 |
|  | lexo | 3.67 | 3.64 | 4.03 | 3.99 | 3.41 |
| Exp. \% |  |  |  |  |  | 100\% (32) ${ }^{\text {a }}$ |

a Ref. 20.
seven orientations give a total of fourteen possible adducts. Furthermore the HOMO of fulvene has zero

Table 13
Transition-state interaction energies (a.u.) for the addition of cyclopentadiene (33) to 1-(pyrimidin-2-yl)-3-oxidopyridinium

| Eqn. | Reaction at 2,6-position of betaine |  | Reaction at 2,4-position |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
|  | [as (26)] | [as (27)] |  |
| (1) | $-0.0409$ | $-0.0386$ | -0.0535 |
| (4) endo | 4.50 | 4.48 | 4.54 |
| lexo | 4.92 | 4.93 | 4.33 |
| Exp. \% | $33 \%$ [as (26a) |  | 67\% exo (34) ${ }^{\text {a }}$ |

$$
{ }^{\sigma} \text { Ref. } 3 .
$$

coefficients at the 1 - and 6 -positions and therefore calculations including the SOMO have also been carried out (Table 14).

Conclusions.-We have demonstrated the FMO method to be a powerful tool for the explanation, rationalisation,



and prediction of peri-, site, regio-, and stereo-selectivity and for the quantitative correlation of kinetic rate data within the various thermal cycloadditions to 3 -oxidopyridiniums.

Table 14
Transition state energies (a.u.) for addition of fulvene (35) to 1-(pyrimidin-2-yl)-3-oxidopyridinium [equation (1)]

| Regioisomer ${ }^{\text {a }}$ | $\mathrm{H}_{\mathrm{B}} \mathrm{L}_{\mathrm{F}}$ | $\mathrm{L}_{\mathrm{B}} \mathrm{H}_{F}$ | $\mathrm{L}_{\mathrm{B}} \mathrm{S}_{\mathrm{F}}$ | T | exo | endo |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2,2'-6,6' | -0.0288 | -0.0073 | -0.0044 | -0.0405 | 5.35 | 4.94 |
| 2,6'-6, $2^{\prime}$ | -0.0342 | -0.0064 | -0.0053 | -0.0459 | 5.39 | 4.82 |
| 2,2'-6,3' | $-0.0174$ | -0.0190 | -0.0044 | -0.0308 | 5.39 | 4.92 |
| 2,3'-6, $2^{\prime}$ | -0.0169 | -0.0186 | -0.0047 | -0.0402 | 5.42 | 4.84 |
| 2,1'-6,6' | $-0.0216$ | $-0.0000$ | -0.0213 | -0.0429 | 4.86 | 4.86 |
| 2,6'-6, $1^{\prime}$ | $-0.0285$ | $-0.0000$ | -0.0216 | -0.0501 | 4.76 | 4.76 |
| 2,2'-4,5' | -0.0174 | -0.0299 | $-0.0000$ | -0.0473 | 4.28 | 4.92 |

[^1] $\left.\mathrm{cm}^{-1}\right]$ were detected.

We cannot presently explain experimental results for the fulvene addition: we believe that the product found

(32)

(33)

(34)
experimentally (36) does not derive from kinetic control, but from (37) by a 1,5 hydrogen shift.

We are grateful to Drs. B. El-Osta and G. Musumarra for help with calculations, and also thank Drs. B. Ibrahim and G. J. Sabongi for helpful discussions.
[7/1598 Received, 8th September, 1977]

## REFERENCES

${ }^{1}$ Part 37, A. R. Katritzky, N. Dennis, and M. Ramaiah, J. Indian Chem. Soc., in the press.
${ }_{2}$ N. Dennis, B. Ibrahim, and A. R. Katritzky, J.C.S. Perkin I, 1976, 2296.
${ }^{3}$ N. Dennis, B. Ibrahim, and A. R. Katritzky, J.C.S. Perkin I, 1976, 2307.
${ }_{4}$ G. Guiheneuf, C. Laurence, and A. R. Katritzky, J.C.S. Perkin II, 1976, 1829.
${ }^{5}$ K. Yakushi, I. Ikemoto, and H. Kuroda, Acta Cryst., 1971, 27B, 1710.
${ }^{6}$ N. A. Ahmed and A. I. Kitaigorodsky, Acta Cryst., 1972, 28B, 739.
${ }_{7}{ }^{\text {D }}$. Belitskus and G. A. Jeffrey, Spectrochim. Acta, 1965, 21, 1563.
${ }^{8}$ P. H. Cureton, C. G. Le Fèvre, and R. J. W. Le Fèvre, $J$. Chem. Soc., 1963, 1736.
${ }^{9}$ I. Crossland, Acta Chem. Scand., 1966, 20, 258.
10 R. Sustmann and H. Trill, Angew. Chem. Internat. Edn., 1972, 11, 838; K. N. Houk, J. Sims, C. R. Watts, and L. J. Luskus, J. A mer. Chem. Soc., 1973, 95, 7301.
${ }^{11}$ G. Klopman, J. Amer. Chem. Soc., 1968, 90, 223; L. Salem, J. Amer. Chem. Soc., 1968, 90, 543.

12 R. Sustmann, Pure Appl. Chem., 1974, 40, 569.
${ }_{13}$ O. Eisenstein and Nguyên Trong Anh, Tetrahedron Letters, 1971, 1191; Bull. Soc. chim. France, 1973, 2721.
14 W. C. Herndon and L. H. Hall, Tetrahedron Letters, 1967, 3095.

15 R. Sustmann and G. Binsch, Mol. Phys., 1971, 20,

16 M. J. S. Dewar and G. Klopman, J. Amer. Chem. Soc., 1967, 89, 3089; R. C. Bingham and M. J. S. Dewar, ibid., 1972, 94 9107.
${ }_{17}$ N. Dennis, A. R. Katritzky, G. J. Sabounji, and L. Turker, J.C.S. Perkin I, 1977, 1930.
${ }_{18}$ N. Dennis, A. R. Katritzky, and G. J. Sabounji, Tetrahedron Letters, 1976, 2959.

19 Unpublished work with Dr. G. Sabongi and Mr. A. Cutler.
${ }^{20}$ Unpublished results with L. Turker.


[^0]:    $\dagger$ Throughout this paper, and particularly in the Tables, whereever the 2 -pyridyl, pyrimidin-2-yl, and triazin-2-yl substituents are referred to, the experimental data actually come from the corresponding 5 -nitro-2-pyridyl, 4,6-dimethylpyrimidin-2-yl, and 4,6 -dimethoxytriazin-2-yl compounds. Similarly for $\beta$-formylvinyl, the experimental data refer to $p$-chlorobenzoylvinyl.

[^1]:    ${ }^{a}$ Exp. 2, $2^{\prime}-6,6^{\prime}, 20 \%(36)$ (ref. 3). Only adducts of the type $2, x-6, y\left[\nu(\mathrm{C}=\mathrm{O}) 1680-1690 \mathrm{~cm}^{-1}\right]$ were formed in the reaction between 6-(4-methoxyphenyl)fulvene and 1 -(pyrimidin-2-yl)-3-oxidopyridinium. No adducts of the type $2,2^{\prime}-4,5^{\prime}[\boldsymbol{\nu}(\mathrm{C}=\mathrm{O})$ 1 740

